

The figurate numbers

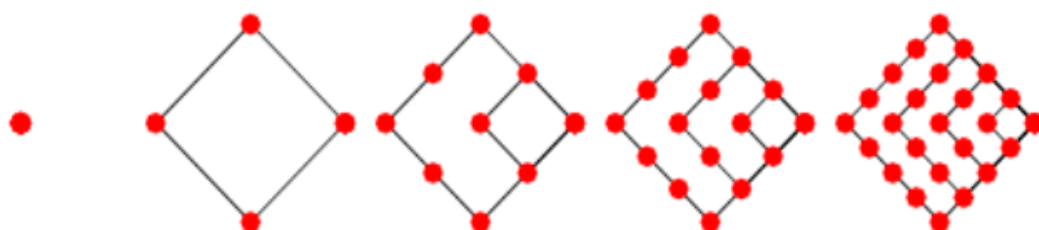
The Natural numbers

and

their geometrical
representations



The Square numbers



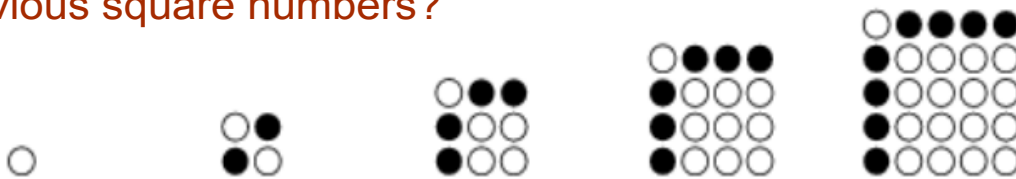
Which numbers are represented here? add others..



for $n=0, 1, \dots$ they are 0, 1, 4, 9, 16, 25, 36, 49, ...
in the relationship:
 $S_n = n^2$

The Square numbers

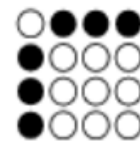
but how is it possible to create a new square number from the previous square numbers?



observe this representation and try to explain it!



type is called gnomon.....



which kind of operation can you do to compose the square number "16"?



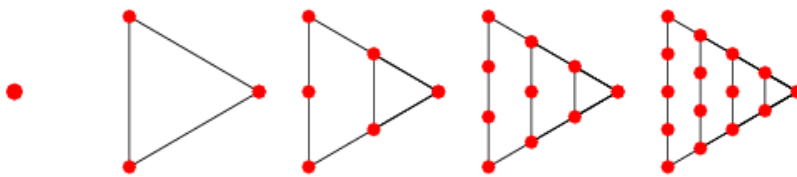
and the way to calculate a "n" square number:



$$(n+1)^2 = n^2 + 2n + 1$$



The triangular numbers



Which numbers are rapresented here? add others..



The triangular numbers are: 1, 3, 6, 10, 15, 21, ...



The triangular numbers

how is possible to obtain these numbers from the natural numbers?



you can do:
1, 1+2, 1+2+3, 1+2+3+4,.....



or like Mathematicians write:



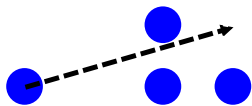
More formally, a triangular number is a number obtained by adding all positive integers less than or equal to a given positive integer n .



Square numbers and triangular numbers

Are there some special relationship between square numbers and triangular numbers ?

how two triangular numbers build a square number:



therefore 4 =

the next combination...:

The rule is....:

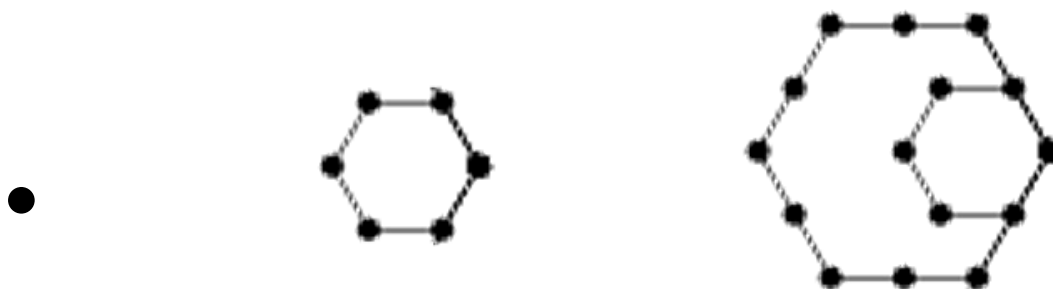


Other figurate numbers

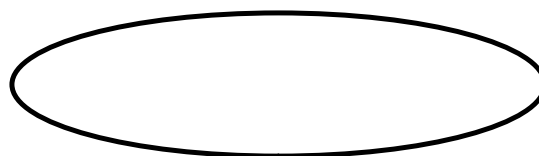
A figurate number, also known as a figural number, is a number that can be represented by a regular geometrical arrangement of equally spaced points.

If the arrangement forms a regular polygon, the number is called a polygonal number.

The polygonal numbers



How can you call these numbers ?

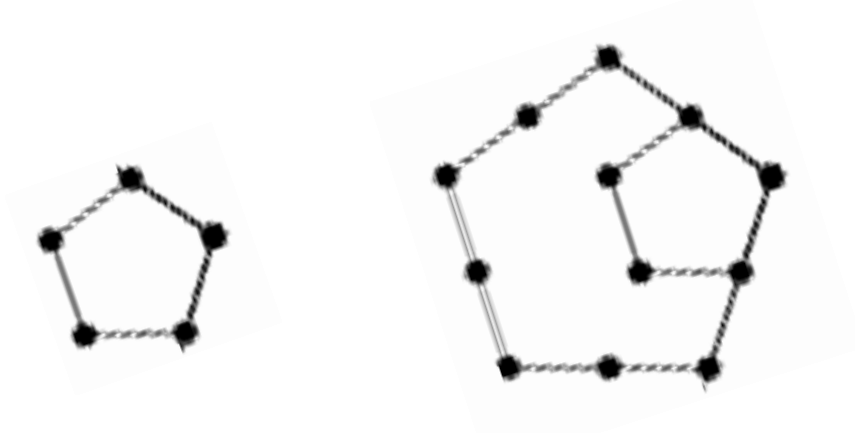


Add other two numbers

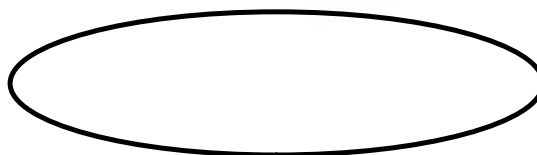


The polygonal numbers

●



How can you call these numbers ?



Add other two numbers



The even numbers

Which geometric representation could the even numbers have?

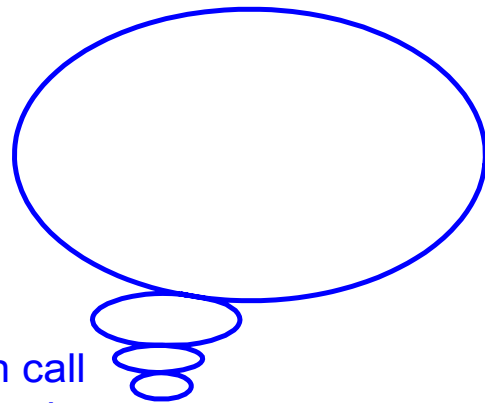


this is 2....

4

6

.....



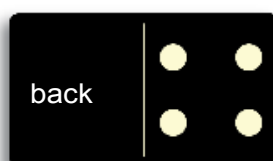
Therefore we can call them: numbers



Teachers' notes

Subject	Arithmetic
Topic	The natural numbers
Title	The figurate numbers

Years	10 -12
Prior knowledge	Operations with the natural numbers
Skills	<ul style="list-style-type: none">• to be able to try the elements of a sequence• to be able to find the rule of the numeric sequence



Notes

In the pages there are some rectangles with the solutions to the questions.

You can read them with a click on the active area.

